## Measuring Time, Space, and Matter

Physics is an experimental science. To understand physics we must be able to connect our theoretical description of nature with our experimental observations of nature. This connection is made through quantitative measurements. To that end, we require some understanding of measurements and how they are made.

## Units of Measurement

In physics, we use several fundamental characteristics to describe nature. We also use certain fundamental units to quantify each characteristic. These characteristics, along with the appropriate units, are listed on the table below.

| SI Fundamental Units |  |  |  |
| :---: | :---: | :---: | :---: |
| Physical Quantity | Quantity Symbol | Unit of Measure | Unit Symbol |
|  |  |  |  |
| length | m | meter | m |
| mass | m | kilogram | kg |
| time | t | second | s |
| charge | Q | Coulomb | C |
|  |  |  |  |

Physical Quantity - any measurable aspect of the universe.
A wide variety of other units, called derived units, are combinations of the base units. For example, speed is a measure of how far an object travels (meters) in a given amount of time (seconds). We measure speed in meters per second $(\mathrm{m} / \mathrm{s})$, a derived unit. Some other common derived units:

| SI Derived Units |  |  |  |  |
| :--- | :--- | :---: | :---: | :---: |
| Quantity | Unit | Symbol | In Base Units | Alternate Units |
| Acceleration |  | $\mathrm{m} / \mathrm{s}^{2}$ | $\mathrm{~m} / \mathrm{s}^{2}$ |  |
| Electric Charge | Coulomb | C | $\mathrm{A} \cdot \mathrm{s}$ |  |
| Electric Field |  | $\mathrm{N} / \mathrm{C}$ | $\mathrm{kg} \cdot \mathrm{m} / \mathrm{C} \cdot \mathrm{s}^{2}$ |  |
| Force | Newton | N | $\mathrm{kg} \cdot \mathrm{m} / \mathrm{s}^{2}$ |  |
| Frequency | Hertz | Hz | s |  |
| Magnetic Field | Tesla | $T$ | $\mathrm{~kg} / \mathrm{A} \cdot \mathrm{s}^{2}$ |  |
| Momentum, Impulse |  | $\mathrm{kg} \cdot \mathrm{m} / \mathrm{s}$ | $\mathrm{kg} \cdot \mathrm{m} / \mathrm{s}$ |  |
| Velocity |  | $\mathrm{m} / \mathrm{s}$ | $\mathrm{m} / \mathrm{s}$ |  |

In physics, we often encounter numbers that are either very large or very small. These numbers can be most easily expressed in one of two ways:

## 1. Scientific Notation

Numbers in scientific notation have the form:

$$
M \times 10^{n}
$$

where $\mathbf{M}$ is a number having a single nonzero figure to the left of the decimal point and $\mathbf{n}$ is a positive or negative exponent.

To write a number in scientific notation:

- Determine $\mathbf{M}$ by shifting the decimal point in the original number to the left or to the right until only one nonzero digit is to the left of it. $\mathbf{M}$ should contain only the significant figures of the original number.
- Determine $\mathbf{n}$ by counting the number of places the decimal has been shifted; if it has been moved to the left, $\mathbf{n}$ is positive; if to the right, $\mathbf{n}$ is negative.
e.g. Speed of Light $=3.00 \times 10^{8} \mathrm{~m} / \mathrm{s}$


## 2. Metric Prefixes

Using scientific notation, 1670 meters can be written as $1.67 \times 10^{3}$ meters. But this same quantity can also be written 1.67 kilometers - abbreviated as 1.67 km . This is an example of using a prefix to indicate a multiple of a base unit. Here the prefix kilo means one thousand or $10^{3}$. The following table gives the prefixes for other common multiples of units:

| Factor | Prefix | Symbol |
| :--- | :--- | :--- |
|  |  |  |
| $10^{12}$ | tera | T |
| $10^{9}$ | giga | G |
| $10^{6}$ | mega | M |
| $10^{3}$ | kilo | k |
| $10^{2}$ | hecto | h |
| $10^{1}$ | deka | da |
| $10^{-1}$ | deci | d |
| $10^{-2}$ | centi | c |
| $10^{-3}$ | milli | m |
| $10^{-6}$ | micro | $\mu$ |
| $10^{-9}$ | nano | n |
| $10^{-12}$ | pico | p |
|  |  |  |

When using numbers with prefixes, they should be converted to scientific notation in the proper units before being used in calculations.

## Unit Conversions

It is often necessary to change from one set of units to another. For example, you may have to convert a given number of seconds into minutes, or a given number of centimeters into meters.

The procedure for converting units involves two steps.

1. Write a conversion factor.
2. Multiply the given set of units by the conversion factor to get the desired set of units.

Several examples of unit conversion will help illustrate this procedure.

## Example \#1

How many millimeters are there in one meter?

## Example \#2

How many nanoseconds are there in one kilosecond? (Hint: It is often necessary to carry out a conversion in two or more steps.)

## Example \#3

An automobile has a speed of $108 \mathrm{~km} / \mathrm{h}$. What is its speed in $\mathrm{m} / \mathrm{s}$ ?

## Example \#4

A bicycle is traveling at a speed of $10 \mathrm{~m} / \mathrm{s}$. What is its speed in $\mathrm{km} / \mathrm{h}$ ?

## Measurement Worksheet

1. Express the following measurements in scientific notation.
a) 5800 m
b) 450000 m
c) 302000000 m
d) 86000000000 m
2. Express the following measurements in scientific notation.
a) 0.000508 kg
b) 0.00000045 kg
c) 0.003600 kg
d) 0.004 kg
3. Express the following measurements in scientific notation.
a) 300000000 s
b) 186000 s
c) 93000000 s
4. Express the following measurements in standard notation.
a) $3.25 \times 10^{8} \mathrm{~kg}$
b) $1.602 \times 10^{-19} \mathrm{C}$
c) 5.0 nanoseconds
5. Convert each of the following length measurements to its equivalent in meters.
a) 1.1 cm
b) 76.2 pm
c) 2.1 km
d) 0.123 Mm
6. Convert each of these mass measurements to its equivalent in kilograms.
a) 147 g
b) $11 \mu \mathrm{~g}$
c) 7.23 Mg
d) 478 mg
7. Express 2500 m in kilometers and in centimeters.
8. One liter ( L ) is a volume of $10^{3} \mathrm{~cm}^{3}$. How many cubic centimeters are in 2.5 milliliters?
9. How many picoseconds are there in 9.2 microseconds?
10. Rank the following mass measurements from smallest to largest: $11.6 \mathrm{mg}, 1021 \mu \mathrm{~g}, 0.000$ $006 \mathrm{~kg}, 0.31 \mathrm{mg}$.
11. How many minutes make a microcentury?
12. When gasoline sells for $\$ 1.069$ per gallon, what is the price in dollars per liter? (1 gallon $=$ 3.7853 L)
13. A clock loses 3.0 s per day. By how many minutes will it be off at the end of one year (365 days)?
14. How many revolutions does the second hand of a clock make in three years? Assume no leap years in the interval.
15. The speed of sound at room temperature is $340 \mathrm{~m} / \mathrm{s}$. Express the speed of sound in units of kilometers per hour.
